



# Relativistic magnetohydrodynamical simulations of the resonant corrugation of a fast shock front

Demidem et al, 2018, Mon. Not. R. Astron. Soc. 475, 2713–2723

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« PIC-MHD simulations of particle acceleration in a magnetized turbulence »

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Isradynamics 2018: Dynamical Processes in Space Plasmas

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# Plan

- I. Introduction: motivations & object of this study
- II. Results from SRMHD simulations of shock interacting with fast magnetosonic or entropy waves
- III. Conclusion

# Motivations

Energy dissipation processes in non-thermal (**relativistic**) sources?

Supernova remnants

IR  
X  
X  
X



Image Credit: MPIA/NASA/Calar Alto Observatory

Active Galactic Nuclei



Image credit: Aurore Simonnet, Sonoma State University

pulsar magnetosphere & nebula

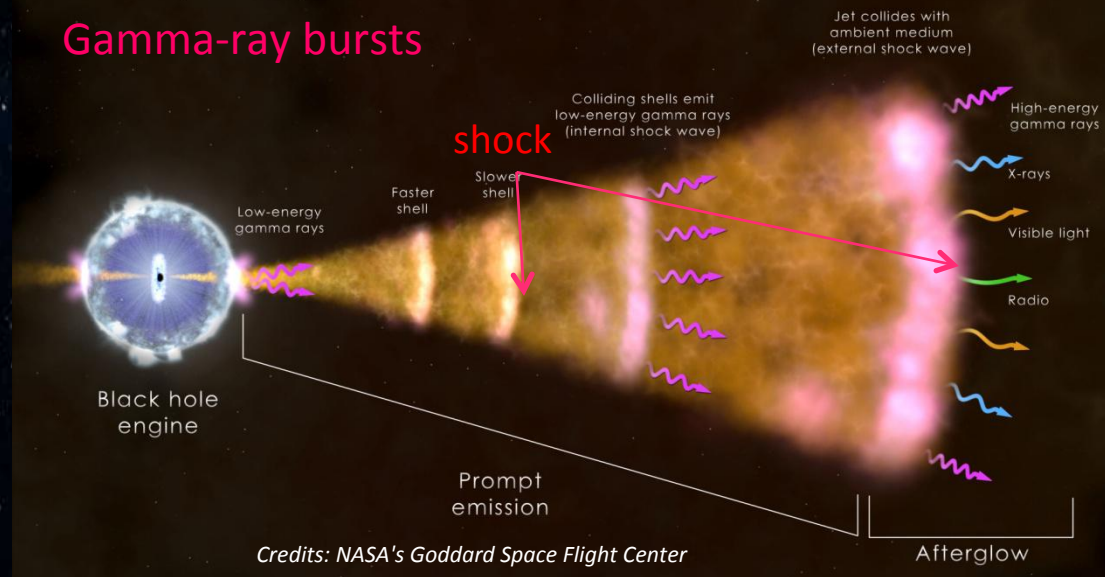
R  
IR  
O  
UV  
X

shock



\*Credits: NASA, ESA, G. Dubner (IAFE, CONICET-University of Buenos Aires) et al.; A. Loll et al.; T. Temim et al.; F. Seward et al.; VLA/NRAO/AUI/NSF, Chandra/CXC, Spitzer/JPL-Caltech; XMM-Newton/ESA; and Hubble/STScI

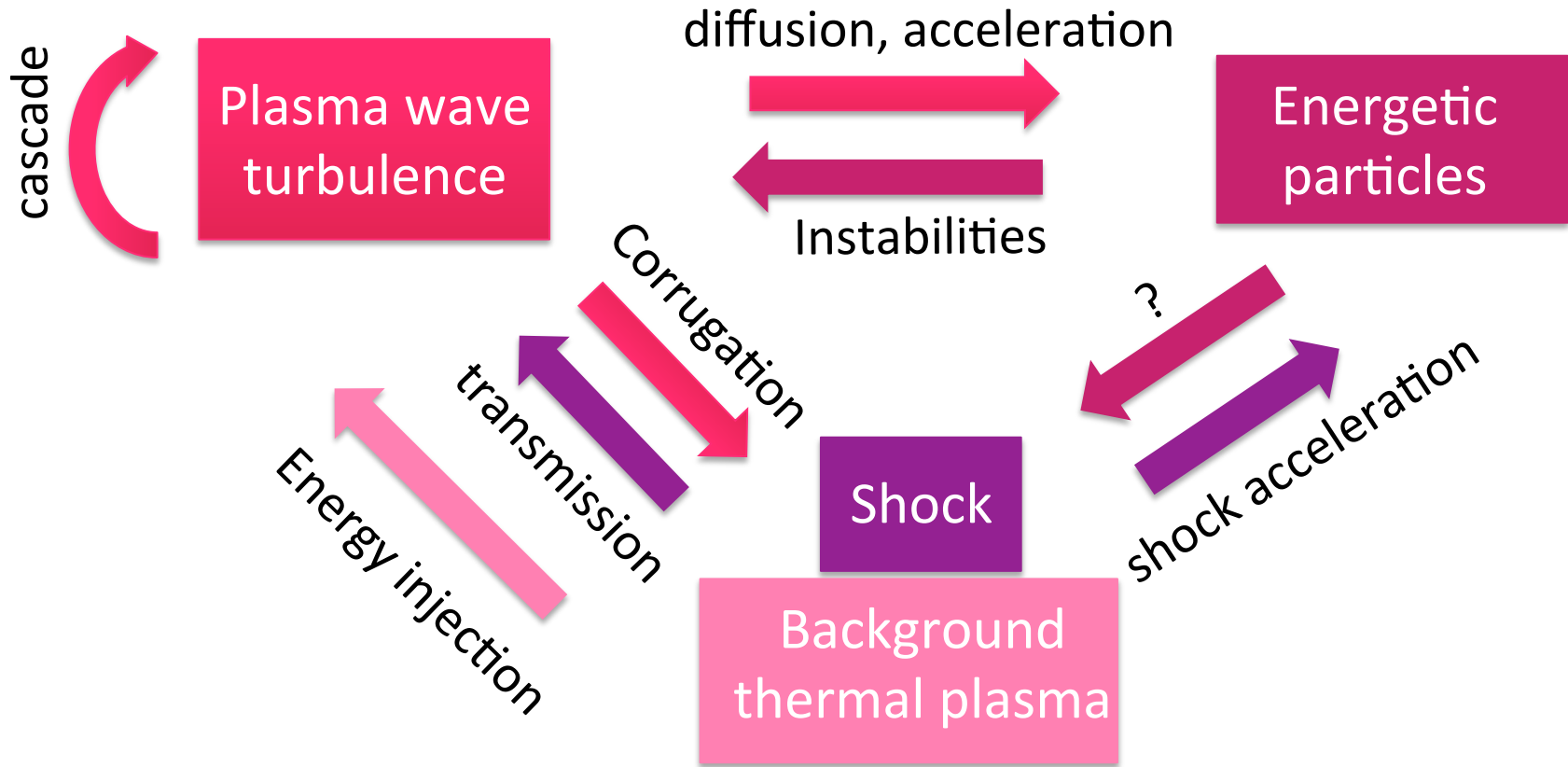
Gamma-ray bursts



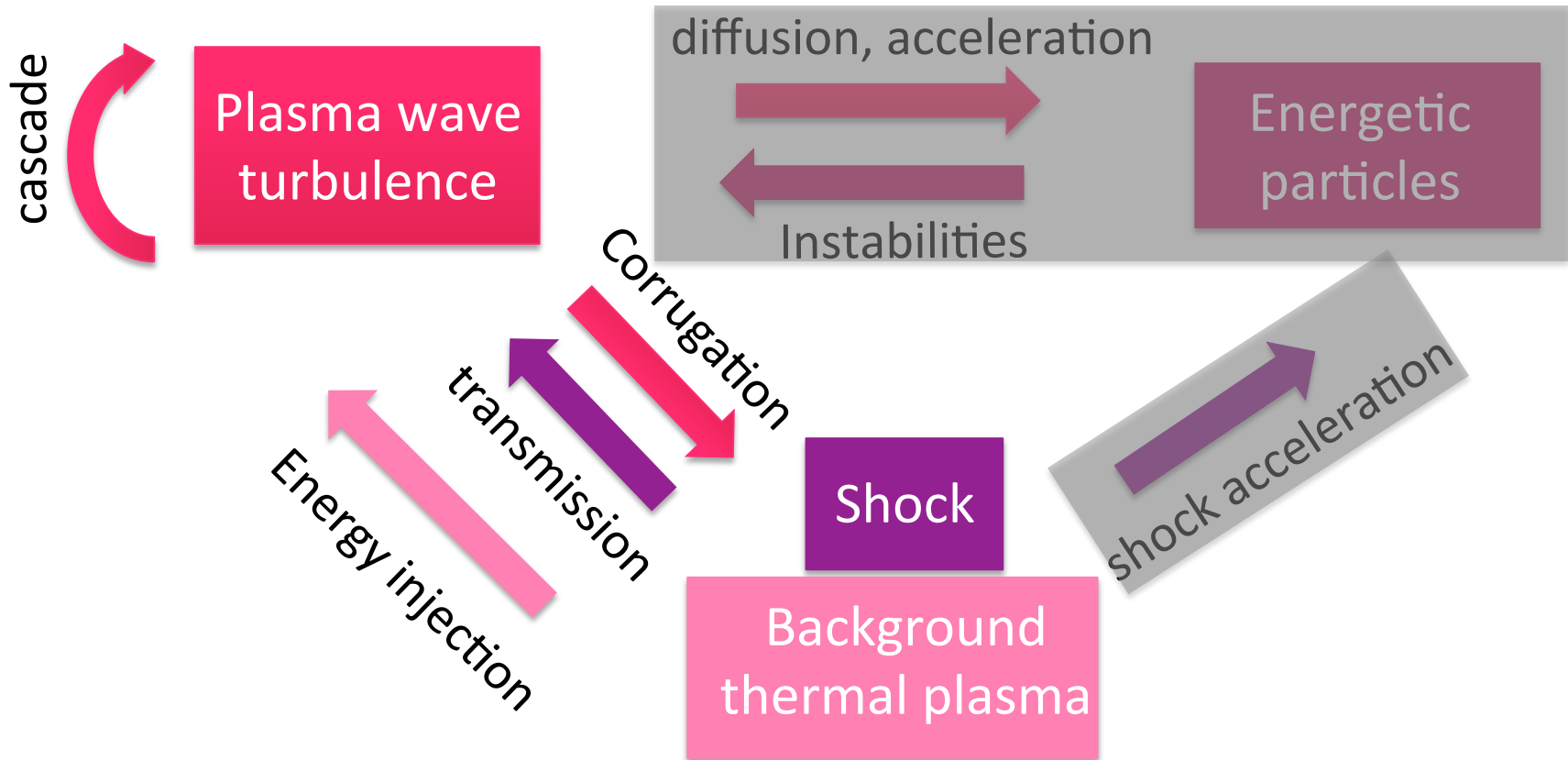
Credits: NASA's Goddard Space Flight Center

Afterglow

# Motivations



# Motivations



- **Next part:** work related to the issue of **shock-turbulence interactions**, in the framework of **MHD**





## Rippled Quasiperpendicular Shock Observed by the Magnetospheric Multiscale Spacecraft

A. Johlander,<sup>1,2</sup> S. J. Schwartz,<sup>3,4</sup> A. Vaivads,<sup>1</sup> Yu. V. Khotyaintsev,<sup>1</sup> I. Gingell,<sup>3</sup> I. B. Peng,<sup>5</sup> S. Markidis,<sup>5</sup> P.-A. Lindqvist,<sup>5</sup> R. E. Ergun,<sup>4</sup> G. T. Marklund,<sup>5</sup> F. Plaschke,<sup>6</sup> W. Magnes,<sup>6</sup> R. J. Strangeway,<sup>7</sup> C. T. Russell,<sup>7</sup> H. Wei,<sup>7</sup> R. B. Torbert,<sup>8</sup> W. R. Paterson,<sup>9</sup> D. J. Gershman,<sup>9,10</sup> J. C. Dorelli,<sup>9</sup> L. A. Avanov,<sup>9</sup> B. Lavraud,<sup>11,12</sup> Y. Saito,<sup>13</sup> B. L. Giles,<sup>9</sup> C. J. Pollock,<sup>9</sup> and J. L. Burch<sup>14</sup>

Collisionless shock nonstationarity arising from microscale physics influences shock structure and particle acceleration mechanisms. Nonstationarity has been difficult to quantify due to the small spatial and temporal scales. We use the closely spaced (subgyroscale), high-time-resolution measurements from one rapid crossing of Earth's quasiperpendicular bow shock by the Magnetospheric Multiscale (MMS) spacecraft to compare competing nonstationarity processes. Using MMS's high-cadence kinetic plasma measurements, we show that the shock exhibits nonstationarity in the form of ripples.



# CRAB FLARES DUE TO TURBULENT DISSIPATION OF THE PULSAR STRIPED WIND

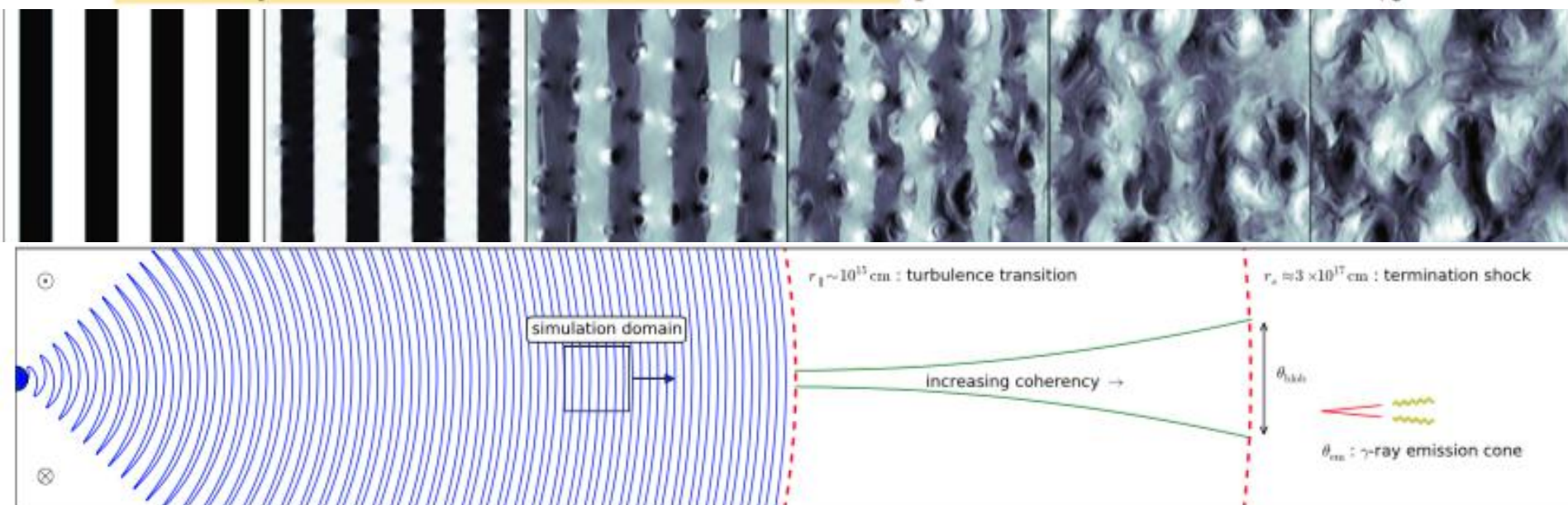
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## ABSTRACT

We interpret  $\gamma$ -ray flares from the Crab Nebula as the signature of turbulence in the pulsar’s electromagnetic outflow. Turbulence is triggered upstream by dynamical instability of the wind’s oscillating magnetic field and accelerates non-thermal particles. On impacting the wind-termination shock, these particles emit a distinct synchrotron component  $F_{\nu, \text{flare}}$ , which is constantly modulated by intermittency of the upstream plasma flow. Flares are observed when the high-energy cutoff of  $F_{\nu, \text{flare}}$  emerges above the fast-declining nebular emission around 0.1–1 GeV. Simulations carried out in the force-free electrodynamics approximation predict the striped wind to become fully turbulent well ahead of the wind-termination shock, provided its terminal Lorentz factor is  $\lesssim 10^4$ .



FFE simulations

# Framework: special relativistic ideal MHD (SRMHD)

- Ideal MHD: fluid description of perfectly conducting plasma
- Governing equations: mass, energy, momentum conservation equations + evolution equation of  $\mathbf{B}$  +  $\text{div}(\mathbf{B})=0$  constraint
- SRMHD  $\rightarrow$  need covariant formalism

Introducing  $b^\mu = [u^i B_i, (\mathbf{B} + u^i B_i \mathbf{u}) / u^0]$ ,

$$c=1, \mu_0=1.$$

$$T^{\mu\nu} = (w + b_\alpha b^\alpha) u^\mu u^\nu + \left( p + \frac{b_\alpha b^\alpha}{2} \right) \eta^{\mu\nu} - b^\mu b^\nu,$$

$$*F^{\mu\nu} = u^\mu b^\nu - u^\nu b^\mu,$$

Notations:

$u^\mu$ : 4-velocity

$\mathbf{B}$ : magnetic field

$p$ : thermal pressure

$w$ : enthalpy density

$\rho$ : proper density

$\eta^{\mu\nu}$ : Minkowsky metric

the governing equations read:  $\nabla_\alpha (\rho u^\alpha) = 0,$

$$\nabla_\alpha T^{\alpha\beta} = 0,$$

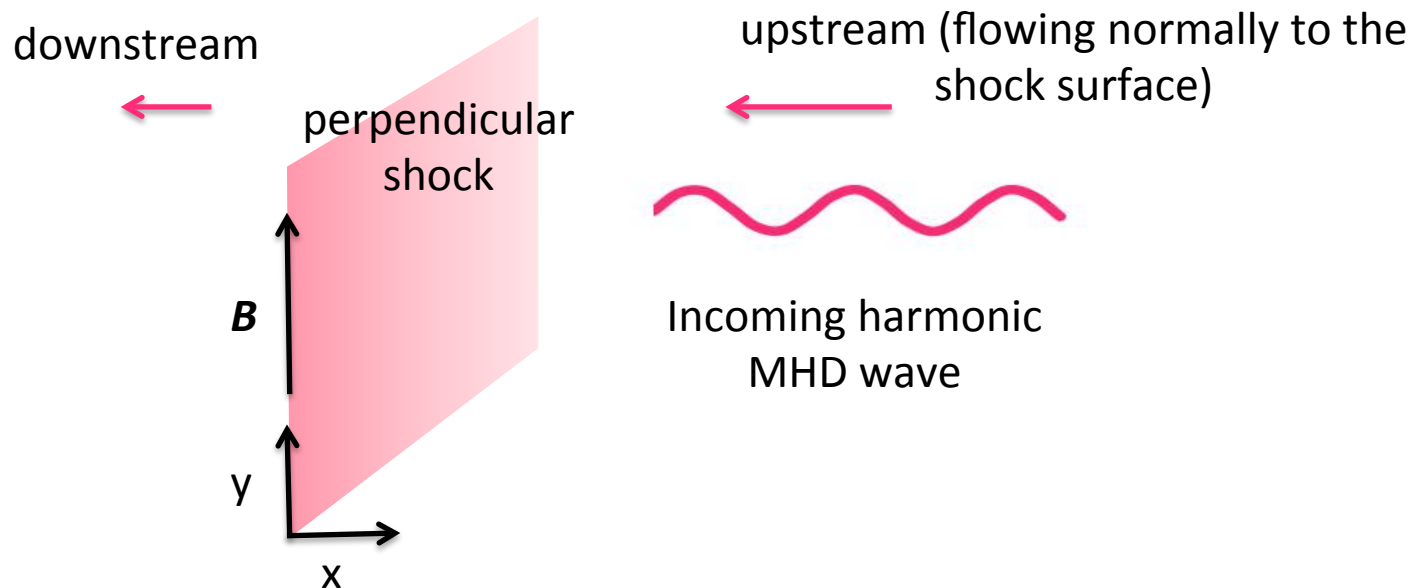
$$\nabla_\alpha *F^{\alpha\beta} = 0.$$

- 7 eigenmodes: 1 entropy + 2 Alfvén + 2 slow magnetosonic + 2 fast magnetosonic



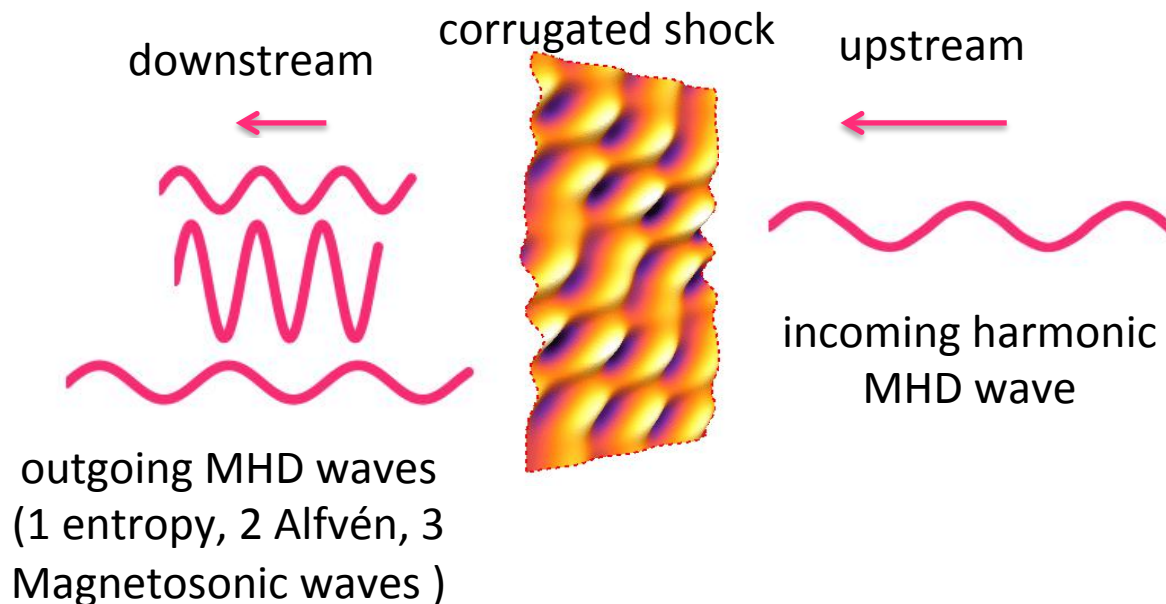
# Framework: shocks interacting with perturbations

- Theoretical study of the linear response of a relativistic shock to an harmonic MHD wave (Lemoine et al, 2016, ApJ 827)



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➔ resonance for some wave vectors.

Observable in simulations of finite amplitude incoming waves?

# Framework: simulation program

**MPI-AMRVAC** (van der Holst et al, 2008, Comp. Phys. Commun., 179, 617)

finite volumes solver + constrained transport algorithm

Updates cell centered quantities by computing flux at the cell borders

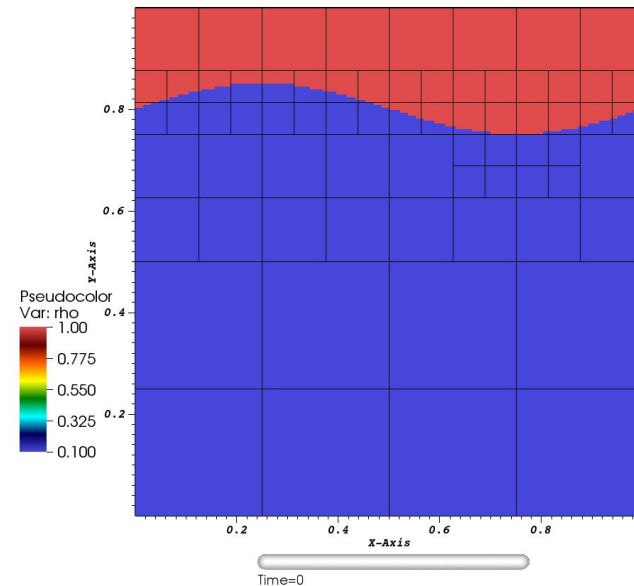
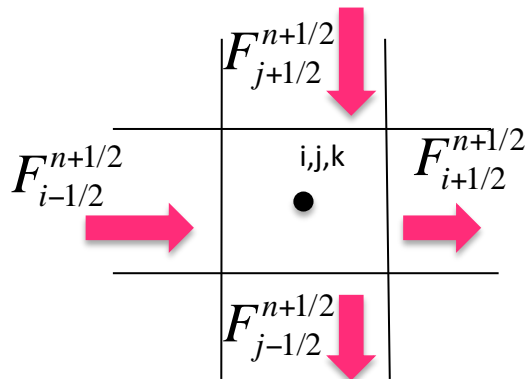
Ensures  $\text{div}(\mathbf{B})=0$

Adaptive Mesh Refinement: adapts grid to zone of interest

$$\frac{\partial D(t, \mathbf{r})}{\partial t} + \nabla \cdot \mathbf{f}(t, \mathbf{r}, D) = 0$$

$$\langle D \rangle_i^{n+1} - \langle D \rangle_i^n + \frac{\Delta t}{\Delta V} (F_{i+1/2}^{n+1/2} - F_{i-1/2}^{n+1/2} + \dots) = 0$$

Volume & time average



Example of simulation of the Rayleigh-Taylor instability

# Initial set up: shock in its rest frame

- 2D problem (incoming wave vector in (x y) plane)
- **Initial state** = solution of the Rankine-Hugoniot jump relations for given upstream state and relative Lorentz factor  $\Gamma_{\text{rel}}$

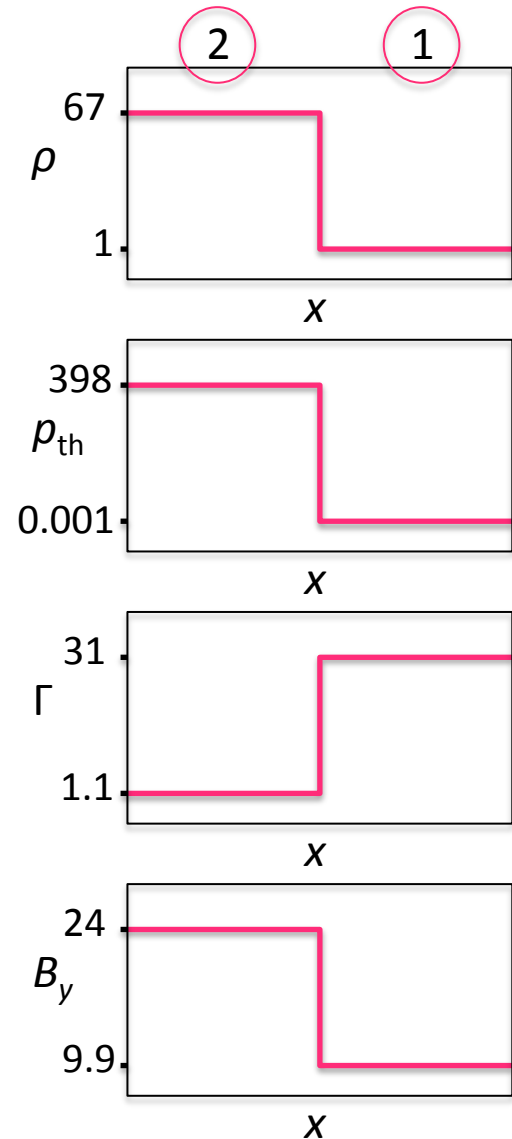
$$\rho_1 \Gamma_1 v_1 = \rho_2 \Gamma_2 v_2$$

$$B_1 v_1 = B_2 v_2$$

$$W_1 \Gamma_1^2 v_1^2 + P_1 = W_2 \Gamma_2^2 v_2^2 + P_2$$

$$W_1 \Gamma_1^2 v_1 = W_2 \Gamma_2^2 v_2$$

with  $P = p_{\text{th}} + B^2/\Gamma^2$ , the total pressure and  $W = w + B^2/\Gamma^2$ , the total enthalpy, associated to an adiabatic ideal gas EOS.

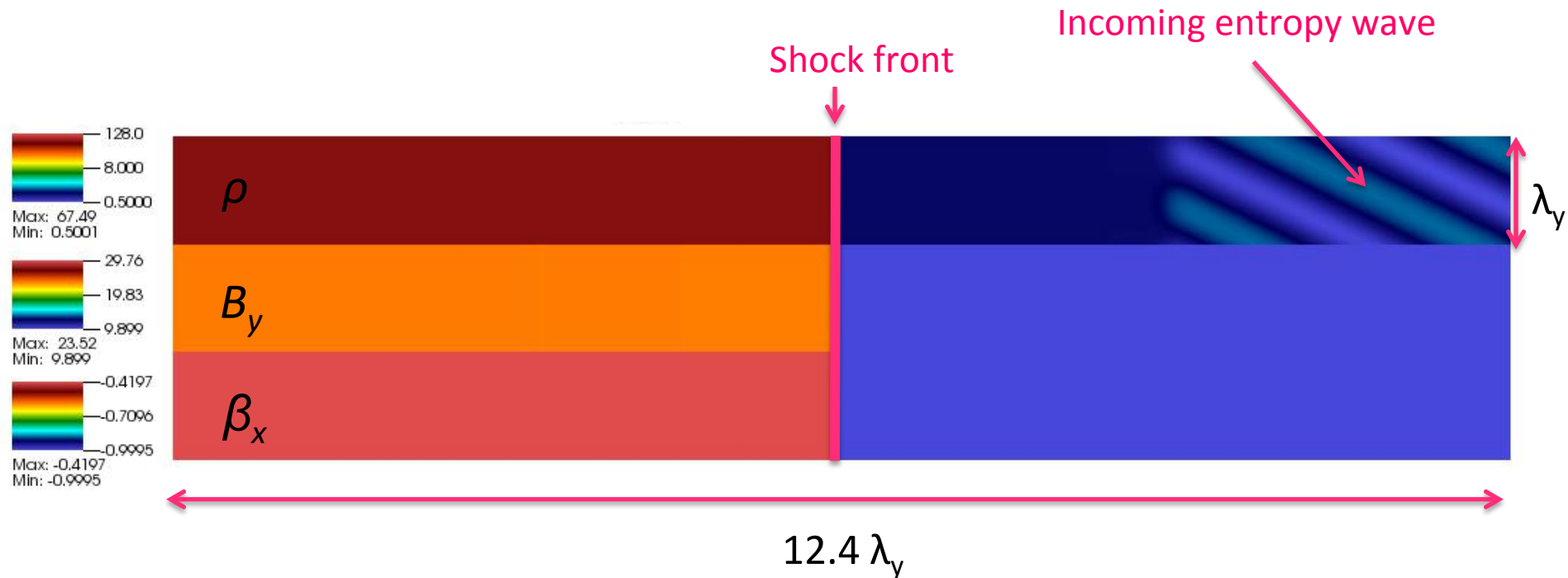




# Relativistic shocks: incoming entropy wave

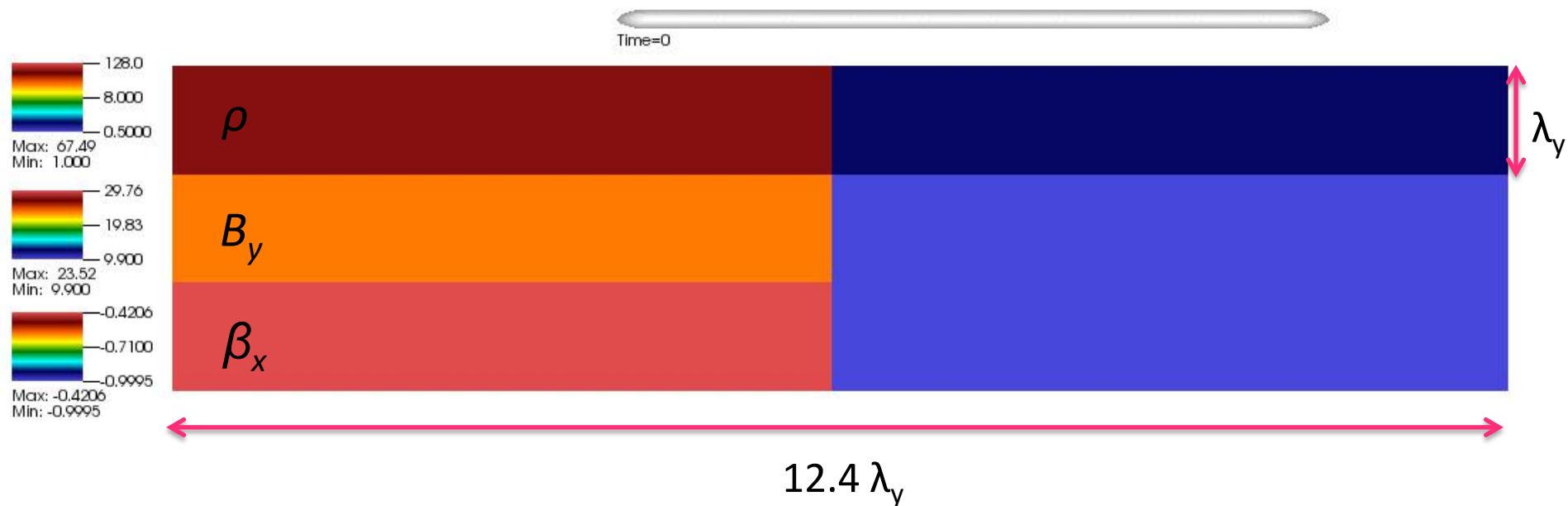
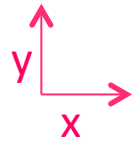
- Entropy wave: perturbations in  $\rho$
- Perturbation amplitude:  $\delta\rho/\rho = 45\%$
- Relative Lorentz factor: 20
- Upstream magnetization:  $\sigma=0.1$

$$\sigma \equiv \frac{\text{magn. energy}}{\text{enthalpy}}$$



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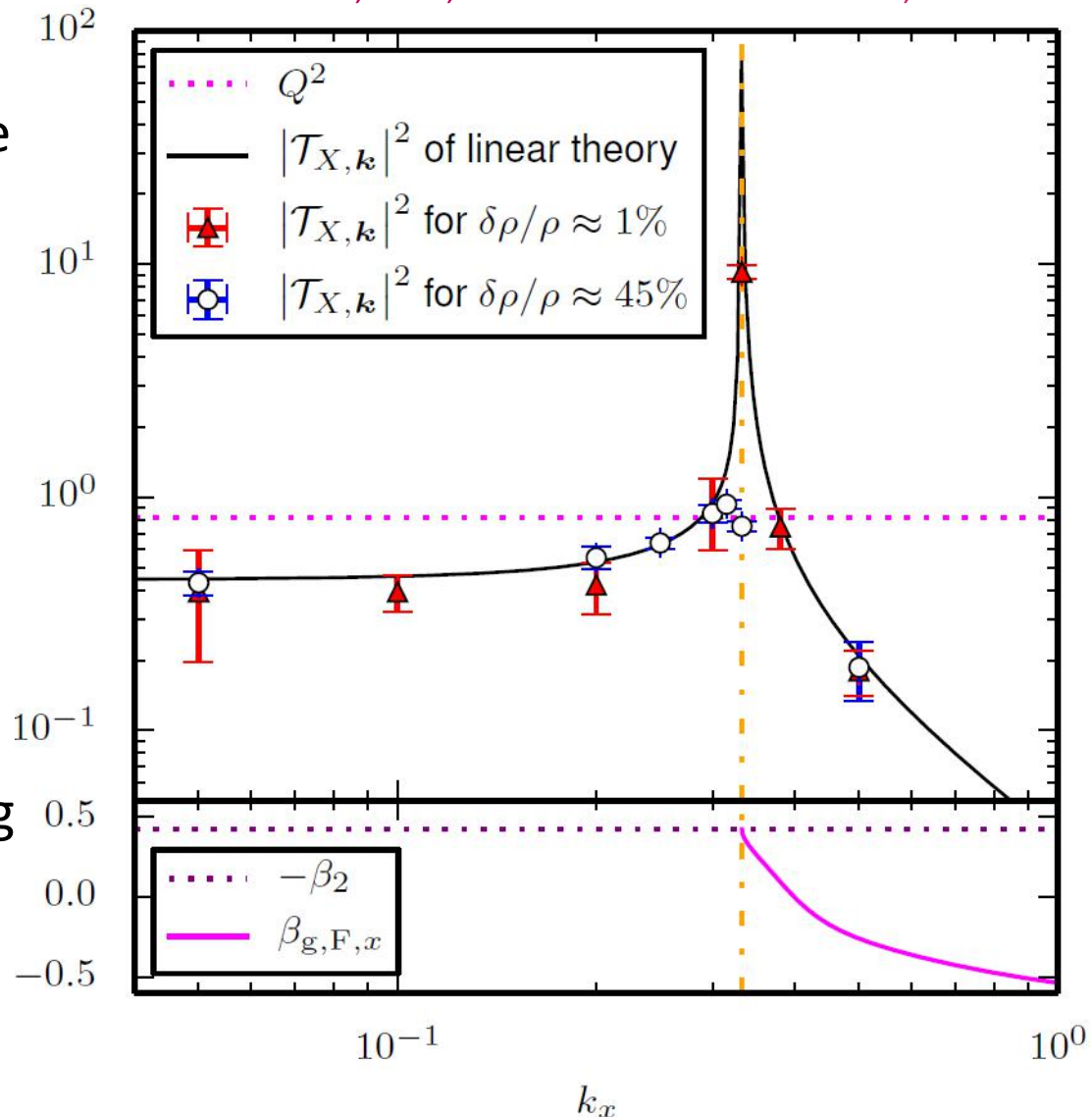
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- In downstream rest frame

- Transfer function

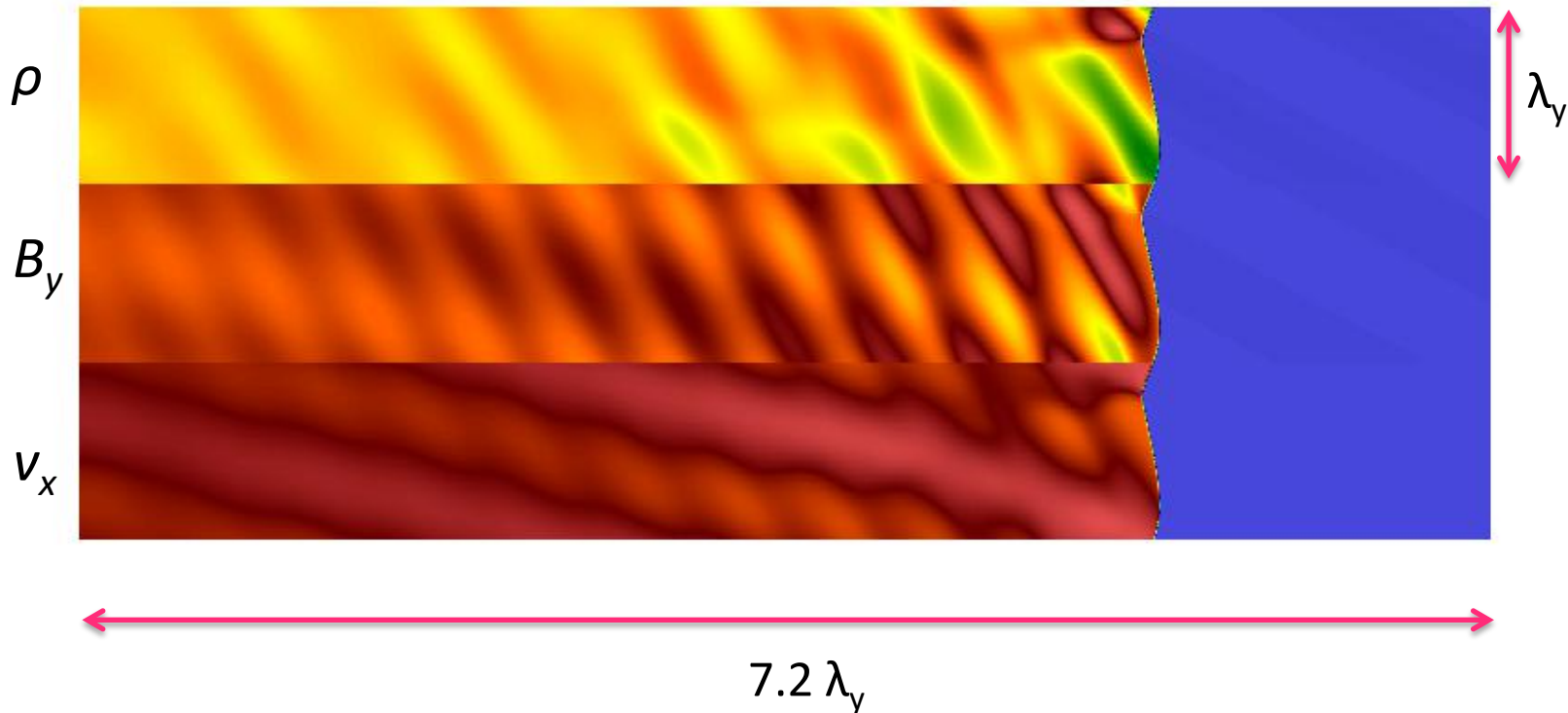
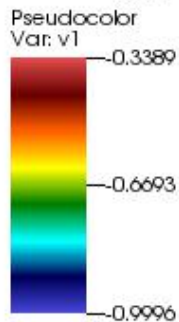
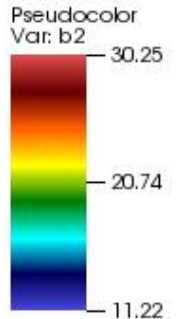
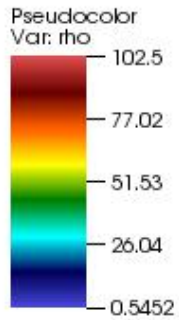
$$\mathcal{T}_{X,k} \propto \frac{\text{ampli of corrugation}}{\text{ampli of wave}}$$

- **Resonance:** longitudinal group velocity of outgoing F mode = shock velocity



# Relativistic shocks: incoming FMS wave

- Perturbation amplitude:  $\delta\rho/\rho = 45\%$
- Relative Lorentz factor: 20
- Upstream magnetization:  $\sigma=0.1$





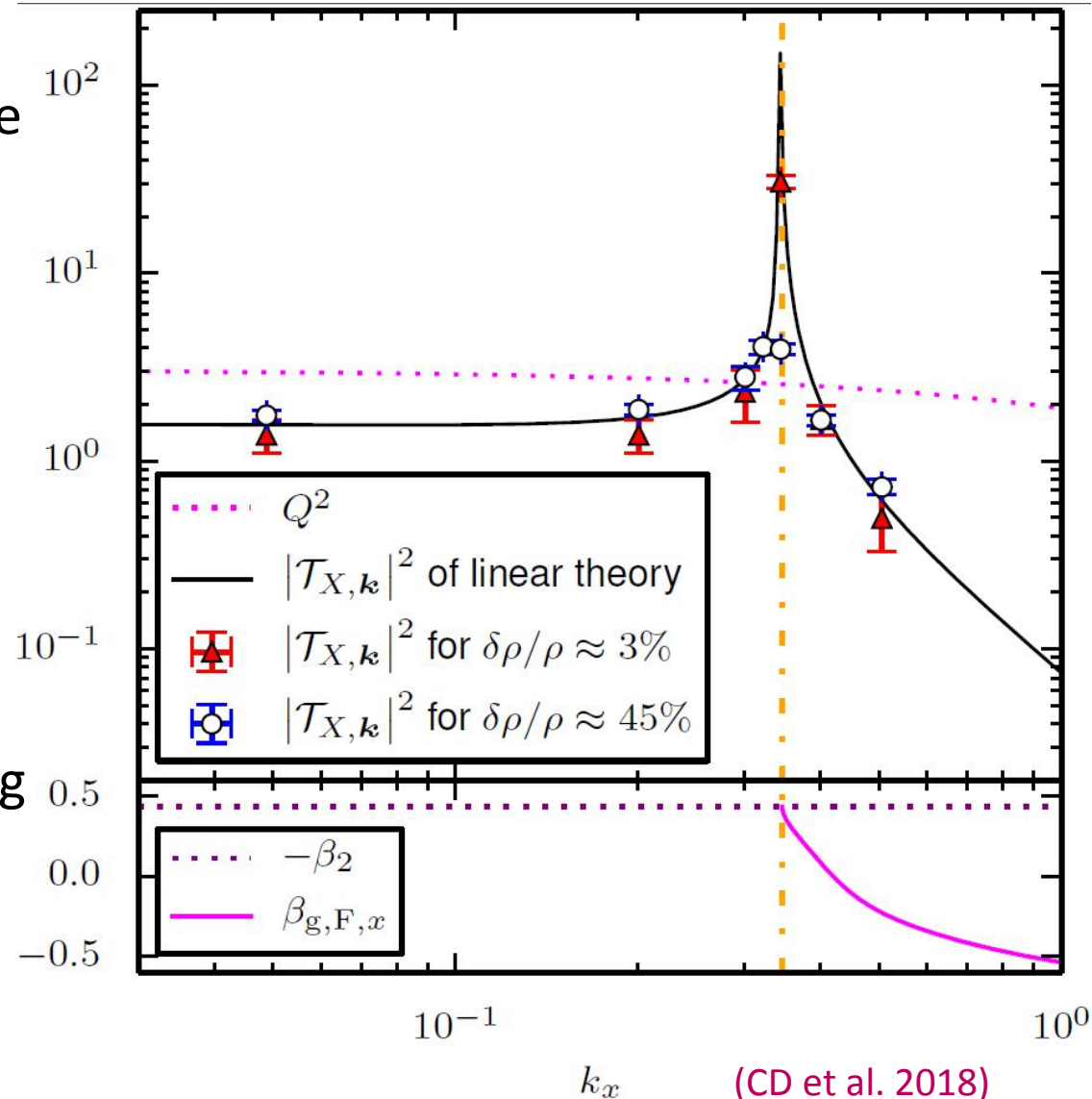
# Relativistic shocks: incoming FMS wave

- In downstream rest frame

- Transfer function

$$\mathcal{T}_{X,k} \propto \frac{\text{ampli of corrugation}}{\text{ampli of wave}}$$

- **Resonance:** longitudinal group velocity of outgoing F mode = shock velocity



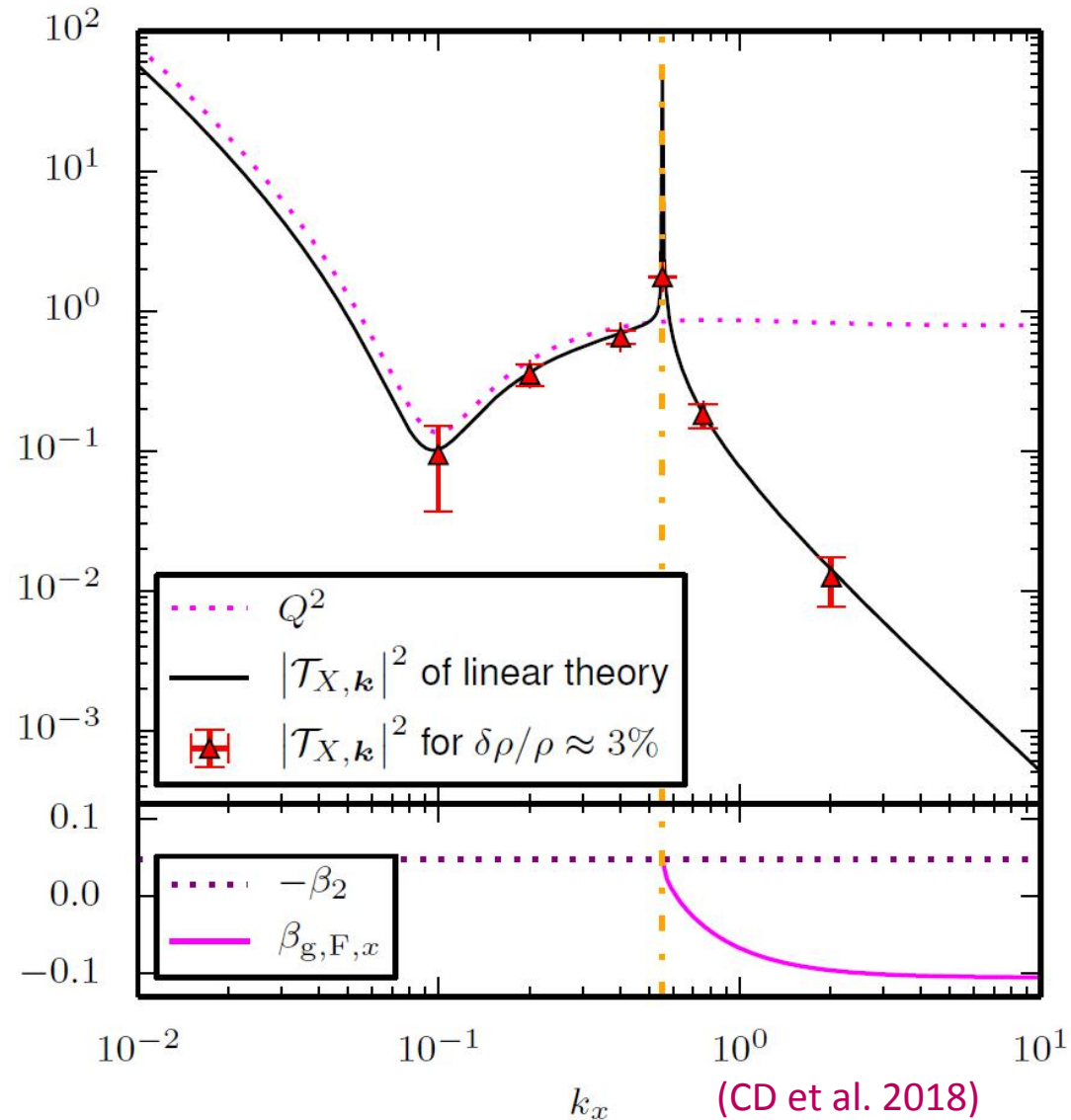
# Sub-relativistic shocks ( $\beta_{\text{sh/up}} \approx 0.2$ , $\sigma \approx 10^{-4}$ ): incoming FMS wave

- In downstream rest frame

- Transfer function

$$\mathcal{T}_{X,k} \propto \frac{\text{ampli of corrugation}}{\text{ampli of wave}}$$

- **Resonance:** longitudinal group velocity of outgoing F mode = shock velocity



# Conclusion

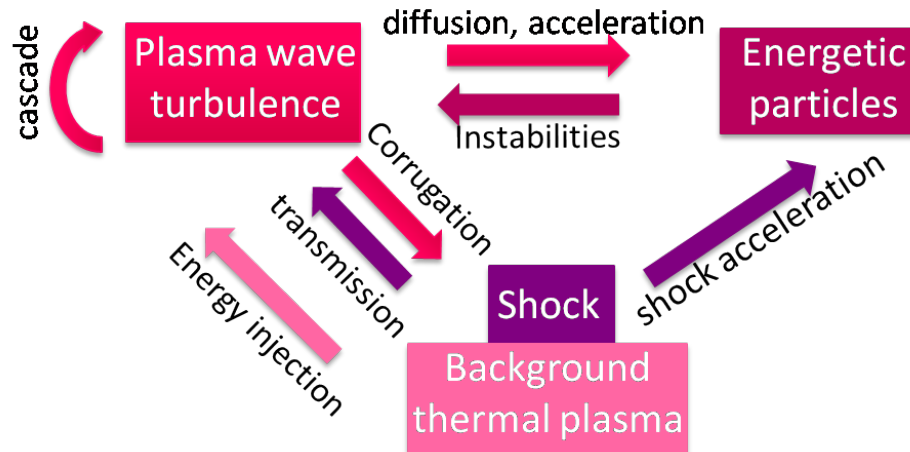
**Summary** (Demidem et al, 2018, Mon. Not. R. Astron. Soc. 475, 2713–2723):

**SRMHD simulations** of interaction of upstream mono $\lambda$  MHD mode with shock show existence of **universal** (i.e. for both relativistic/sub-relativistic velocities & strong/weak magnetizations) **resonant response of shock** to perturbations.

# Conclusion

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**SRMHD simulations** of interaction of upstream mono $\lambda$  MHD mode with shock show existence of **universal** (i.e. for both relativistic/sub-relativistic velocities & strong/weak magnetizations) **resonant response of shock** to perturbations.



## Outlook:

- Impact of the corrugation on particle acceleration?
- PI[MHD]C simulations of **non-relativistic** shocks:  $\rightarrow$  corrugation induced by the accelerated particles which in turn affect particle acceleration efficiency. (Van Marle et al. 2018, MNRAS Vol. 473, 3394)