## **Exercises in Statistical Mechanics**

Based on course by Doron Cohen, has to be proofed Department of Physics, Ben-Gurion University, Beer-Sheva 84105, Israel

This exercises pool is intended for a graduate course in "statistical mechanics". Some of the problems are original, while other were assembled from various undocumented sources. In particular some problems originate from exams that were written by B. Horovitz (BGU), S. Fishman (Technion), and D. Cohen (BGU).

= [Exercise 6020]

## A divided box with a hole in one side

A cylinder of length L and cross section A is divided into two compartments by a piston. The piston has mass M and it is free to move without friction. Its distance from the left basis of the cylinder is denoted by x. In the left side of the piston there is an ideal Bose gas of  $N_a$  particles with mass  $\mathbf{m}_a$ . In the right side of the piston there is an ideal Bose gas of  $N_b$  particles with mass  $\mathbf{m}_b$ . The temperature of the system is T. Assume that the left gas can be treated within the framework of the Boltzmann approximation. Assume that the right gas is in condensation. In items (3-5) consider separately two cases:

(a) A small hole is drilled in the left wall of the box.

(b) A small hole is drilled in the right wall of the box.

The area of the hole is  $\delta A$ .

- (1) Find the equilibrium position of the piston.
- (2) What is the frequency of small oscillations of the piston.
- (3) What is the velocity distribution N(v) of the emitted particles?
- (4) What is the flux (particles per unit time) of the emitted particles?
- (5) Is the piston going to move? If yes write an expression for its velocity.

In item (3) use normalization that makes sense for the calculation in item (4). In item (5) assume that the process is quasi-static, such that at any moment the system is at equilibrium. Express your answers using  $L, A, \delta A, N_a, N_b, \mathsf{m}_a, \mathsf{m}_b, T, M$ .